

# Camera calibration theory

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## Abstract

Summary of key concepts on camera calibration theory

## 1 Introduction

Based on the OpenCV documentation [1].

Consider a point P in 3D with coordinates X in the world reference frame, stored in the matrix X. The coordinate vector of P in the camera reference frame is given by:

$$X_c = R \cdot X + T$$

where R is the rotation matrix corresponding to the rotation vector om, and  $R = \text{rodrigues}(om)$ . Let  $x$ ,  $y$ , and  $z$  represent the three coordinates of  $X_c$ :

$$x = X_{c1}, \quad y = X_{c2}, \quad z = X_{c3}$$

The pinhole projection coordinates of P are  $[a, b]$ , where:

$$a = \frac{x}{z}, \quad b = \frac{y}{z}$$

Using the radial distance  $r^2 = a^2 + b^2$ , the angle  $\theta = \text{atan}(r)$ .

Fisheye distortion:

The angle  $\theta_d$  after distortion is given by:

$$\theta_d = \theta (1 + k_1\theta^2 + k_2\theta^4 + k_3\theta^6 + k_4\theta^8)$$

The distorted point coordinates are  $[x', y']$ , where:

$$x' = \frac{\theta_d}{r} \cdot a, \quad y' = \frac{\theta_d}{r} \cdot b$$

Finally, converting into pixel coordinates: The final pixel coordinates vector  $[u, v]$  are obtained as follows:

$$u = f_x (x' + \alpha y') + c_x, \quad v = f_y y' + c_y$$

This represents a generic camera model [116] with perspective projection and without distortion correction.

Please note that I assumed  $f_x$ ,  $f_y$ ,  $c_x$ , and  $c_y$  as the focal lengths and principal point coordinates of the camera, and  $k_1$ ,  $k_2$ ,  $k_3$ , and  $k_4$  as the distortion coefficients. You can replace these variables with their actual values when using the equations.

$$\begin{bmatrix} u_x \\ u_y \end{bmatrix} = \frac{\theta (1 + k_1\theta^2 + k_2\theta^4 + \dots)}{r} \begin{bmatrix} f_x & 0 \\ 0 & f_y \end{bmatrix} \begin{bmatrix} x/z \\ y/z \end{bmatrix} + \begin{bmatrix} o_x \\ o_y \end{bmatrix} \quad (1)$$

## References

[1] Fisheye opencv docs.